

10 Boolean logic

Name: _____ Class: _____ Date: _____ **Total: 24 marks**

KEY WORDS logic gate • truth table • logic expression • AND • XOR

Objective

Build the skills to answer exam questions on **Boolean logic** : the logic gates NOT, AND, OR, NAND, NOR and XOR, logic expressions, and truth tables for circuits with up to three inputs and one output.

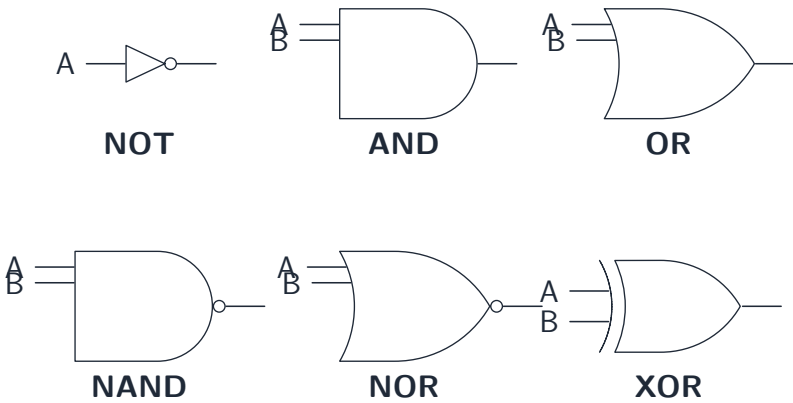
You must be able to:

- state the output of each gate
- write a logic expression from a short problem statement
- complete a truth table from an expression, without simplifying the expression

1 Key knowledge and worked examples

■ The six gates

A **logic gate** takes inputs that are **1** (true) or **0** (false) and gives one output. NOT has one input. The other gates have two inputs at IGCSE.



A small circle on the output means the result is inverted

Gate	Output is 1 when
NOT	the input is 0
AND	both inputs are 1
OR	at least one input is 1
NAND	AND would be 0 (NOT AND)
NOR	OR would be 0 (NOT OR)
XOR	the two inputs are different

AND outputs:

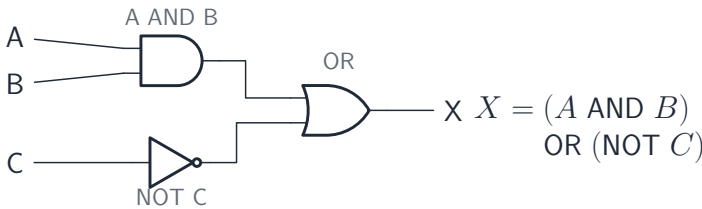
A	B	A AND B
0	0	0
0	1	0
1	0	0
1	1	1

NOR outputs (the opposite of OR):

A	B	A NOR B
0	0	1
0	1	0
1	0	0
1	1	0

■ Expressions and truth tables

A **logic expression** writes the gates in words, such as (A AND B) OR (NOT C). Draw or complete the table for that expression. Do not simplify it first.



Work one gate at a time: AND and NOT first, then OR

3 inputs $\Rightarrow 2 \times 2 \times 2 = 8$ rows

A	B	C
0	0	0
0	0	1
0	1	0
0	1	1
1	0	0
1	0	1
1	1	0
1	1	1

list **every** combination -
count up in binary,
from 000 to 111
the last column flips
every row, the next
every two rows,
the first every four

Two inputs need 4 rows; three inputs need 8 rows

- Worked example.** One row of $X = (A \text{ AND } B) \text{ OR } (\text{NOT } C)$, with $A = 1, B = 0, C = 0$.
- $A \text{ AND } B = 1 \text{ AND } 0 = 0$, because AND needs both inputs to be 1.
 - $\text{NOT } C = \text{NOT } 0 = 1$.
 - $X = 0 \text{ OR } 1 = 1$.

Give each gate its own column. The final column is the output.

2 Practice

- 2.1 Give the output of NOT A when A is 0, and when A is 1.

[2]
- 2.2 State the only input pair that makes an AND gate output 1.

[1]
- 2.3 State when an XOR gate outputs 1.

[1]
- 2.4 Explain what a NAND gate does, and give its output when both inputs are 1.

[2]

2.5 Complete the outputs of $X = A \text{ NOR } B$.

[4]

A	B	X
0	0	
0	1	
1	0	
1	1	

2.6 An alarm X sounds when the door is open (A) AND the system is on (B). Write the logic expression for X.

[2]

3 Exam-style questions

3.1 The gate that outputs 1 only when both inputs are 1 is:

[1]

- ☐

A OR
B XOR
C AND
D NOR

3.2 Complete the truth table for $X = \text{NOT } (A \text{ OR } B)$.

[4]

A	B	A OR B	X
0	0		
0	1		
1	0		
1	1		

3.3 A lamp X is on when switch A is on AND switch B is off.

(a) Write the logic expression for X. Do not simplify a different expression into this one.[2]

(b) Find X when $A = 1$ and $B = 0$. Show the output of each gate. [2]

3.4 $X = (A \text{ AND } B) \text{ OR } C$.

(a) State how many rows a full truth table for A, B and C must have. [1]

(b) Find X when $A = 1$, $B = 1$ and $C = 0$. Show the AND result, then the OR result.[2]
