

Measurement loading, amplifier gain and detector response

GRE · GRE Subject Test · GRE Physics

A voltmeter changes the circuit it measures; the reading is a divider output, not the open-circuit voltage.

Prerequisites: 14, 21, 30.

- Calculate measurement loading from finite meter and source impedances
- Determine simple amplifier gain and first-order filter response
- Interpret detector efficiency, resolution, dead time and calibration bias

Model the measurement

Model the measured circuit as a Thevenin source V_{th} with resistance R_{th} and the instrument as input resistance R_m . The reading is $V_{th} \cdot R_m / (R_m + R_{th})$, with the same sign as V_{th} and magnitude no greater than $|V_{th}|$ for positive resistances. A 10 V source with $R_{th}=100\text{ k}\Omega$ read by a 1 M Ω meter gives $10 \times (1/1.1) = 9.09\text{ V}$, a 9% low bias. A $10\times$ oscilloscope probe raises the effective input resistance and divides the signal by ten; quote both effects.

Set gain and cutoff

An ideal non-inverting op-amp stage has gain $1+R_2/R_1$; the inverting stage has $-R_2/R_1$, with the sign carried explicitly. A first-order RC low-pass has cutoff $f_c = 1/(2\pi RC)$; its amplitude ratio is $1/\sqrt{1+(f/f_c)^2}$ and its phase is $-\arctan(f/f_c)$. At $f=f_c$ the amplitude is $1/\sqrt{2}$ (the -3 dB point), not one half. For $R=1\text{ k}\Omega$ and $C=100\text{ nF}$, $f_c \approx 1.59\text{ kHz}$.

Rate the detector

Detector efficiency ε is detected events divided by incident events; energy resolution is quoted as FWHM/E , such as 13.2 keV on a 662 keV line, about 2%. A non-paralyzable detector with dead time τ records $m = n/(1+n\tau)$ from true rate n ; inverting gives $n = m/(1-m\tau)$, which fails as $m\tau \rightarrow 1$. State which dead-time model you assume; paralyzable behaviour differs.

Calibrate with its limits

A linear calibration against known standards can correct offset and scale error; it does not remove noise or guarantee correction of nonlinearity. A calibration curve maps indicated to true values; interpolation between points assumes local smoothness. Report resolution and efficiency separately: sharp peaks with poor efficiency still miss events, and high efficiency with broad resolution still mixes nearby lines.

Worked method

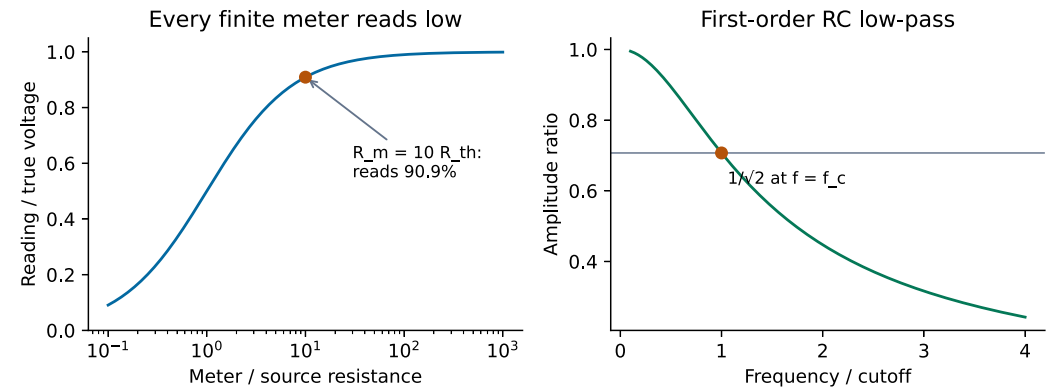
A voltmeter of finite input resistance forms a divider with the source resistance.

$$V_m = V_{th} \frac{R_m}{R_m + R_{th}} = (12\text{ V}) \frac{1.0\text{ M}\Omega}{1.0\text{ M}\Omega + 0.20\text{ M}\Omega} = 10.0\text{ V}.$$

For a nonparalysable detector with observed rate m and dead time τ ,

$$n = m/(1 - m\tau), \quad m\tau < 1.$$

Efficiency, dead time and spectral resolution are different corrections; one cannot replace the others.



Measurement loading, amplifier gain and detector response: original GRE teaching diagram.

Check conditions and vocabulary

Treating the $1/\sqrt{2}$ cutoff as one half, ignoring that a finite meter reads low through the divider, or applying the non-paralyzable correction beyond its range.

dead time: The minimum interval after one recorded event during which the detector cannot record another.

input impedance : The effective load a measuring instrument presents to the circuit under test.