

# Fluids

## AP Physics 1

### Internal Structure and Density

The differences between solids, liquids, and gases come from how strongly their particles interact. A **fluid** 流体 (liquid or gas) has no fixed shape – it flows because its particles move past one another. **Density** 密度 is mass per unit volume:

$$\rho = \frac{m}{V}.$$

It depends on the substance and its state. An object sinks or floats depending on how its density compares with the surrounding fluid's – less dense floats, more dense sinks. An **ideal fluid** 理想流体 is **incompressible** 不可压缩 (constant density, whatever the pressure) and has no **viscosity** 黏度 (internal friction) – the model AP uses throughout.

### Pressure

**Pressure** 压强 is the perpendicular force per unit area, a **scalar** 标量 measured in pascals (Pa):

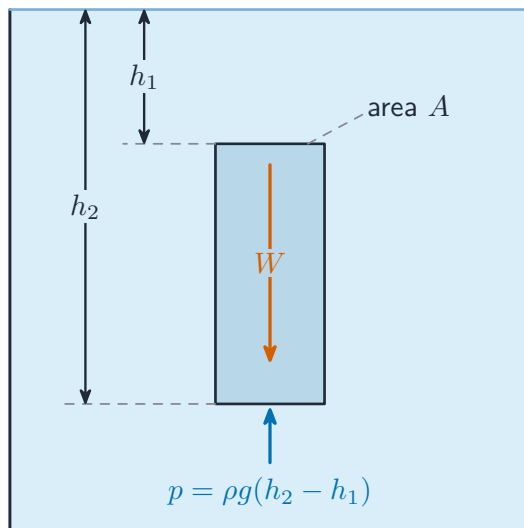
$$P = \frac{F_{\perp}}{A}.$$

In a fluid at rest, pressure increases with **depth** 深度 because of the weight of fluid above:

$$P = P_0 + \rho gh,$$

where  $P_0$  is the pressure at the surface and  $h$  is the depth. Pressure acts **equally in all directions** at a point and pushes **perpendicular** to any surface.

Distinguish the two pressures AP asks about: the **gauge pressure** 表压 is the extra pressure the fluid column adds,  $P_{\text{gauge}} = \rho gh$ , while the **absolute pressure** 绝对压强 is the total,  $P = P_0 + P_{\text{gauge}}$  (with  $P_0$  usually atmospheric). A tyre gauge reading "200 kPa" is gauge pressure; the air inside is really at about 300 kPa absolute.



*The weight of a liquid column sets the extra pressure at a depth*

**Worked example.** Find the total pressure on a diver 10 m below the surface of water ( $\rho = 1000 \text{ kg/m}^3$ , surface pressure  $P_0 = 1.0 \times 10^5 \text{ Pa}$ ):

$$P = P_0 + \rho gh = 1.0 \times 10^5 + 1000 \times 9.8 \times 10 = 1.98 \times 10^5 \text{ Pa}.$$

Every 10 m of water adds roughly one extra atmosphere of pressure. Notice the pressure does not depend on the shape or width of the container, only on the depth.



*An aneroid barometer measures air pressure with a sealed metal box that flexes as the pressure outside changes*

# Fluids and Newton's Laws

An object in a fluid feels an upward **buoyant force** 浮力 equal to the weight of the fluid it displaces – **Archimedes' principle** 阿基米德原理:

$$F_b = \rho_{\text{fluid}} g V_{\text{displaced}}.$$

Combine this with Newton's laws: the object floats when buoyancy balances weight, sinks when weight wins, and rises when buoyancy wins. A floating object displaces exactly its own weight of fluid.

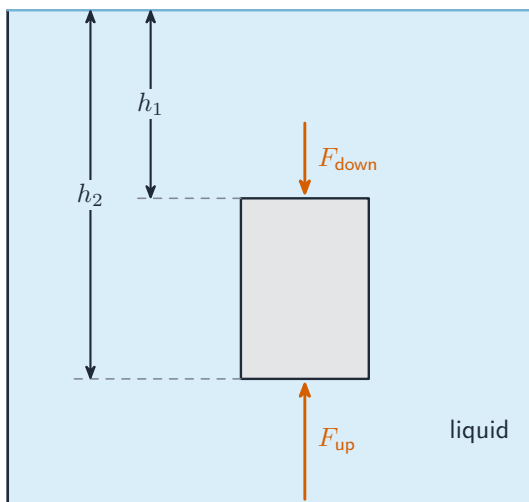
**Worked example.** A block of density  $600 \text{ kg/m}^3$  floats in water ( $1000 \text{ kg/m}^3$ ). What fraction is under the surface? For floating, the buoyant force equals the weight, so  $\rho_{\text{fluid}} g V_{\text{sub}} = \rho_{\text{object}} g V$ :

$$\frac{V_{\text{sub}}}{V} = \frac{\rho_{\text{object}}}{\rho_{\text{fluid}}} = \frac{600}{1000} = 0.60.$$

So 60% sits below the water – the same reason most of an iceberg (density  $\approx 900$ ) hides underwater.

# Fluids and Conservation Laws

For an ideal fluid flowing steadily, two conservation ideas apply:



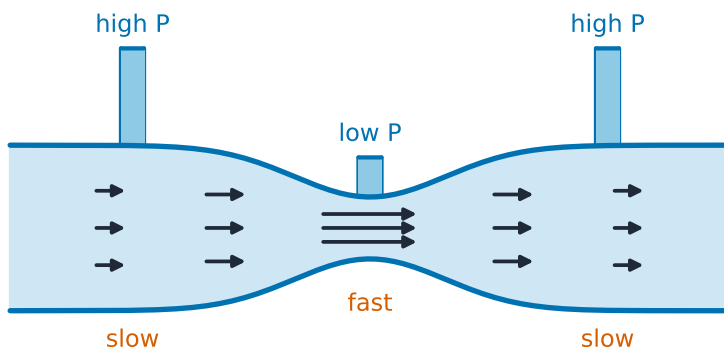
*Upthrust arises because the pressure on the bottom of an object exceeds that on the top*

- **Continuity** 连续性 (conservation of mass): the volume flow rate is constant, so  $A_1 v_1 = A_2 v_2$ . A narrower pipe forces **faster** flow.

- **Bernoulli's equation** 伯努利方程 (conservation of energy per volume): along a streamline,

$$P + \frac{1}{2}\rho v^2 + \rho gy = \text{constant}.$$

Together they explain why fluid speeds up and its pressure drops where a pipe narrows or where flow is fastest.



$$A_1 v_1 = A_2 v_2 \quad \cdot \quad P + \frac{1}{2}\rho v^2 = \text{const (horizontal)}$$

*Where the pipe narrows the fluid speeds up (continuity) and its pressure drops (Bernoulli)*

**Worked example.** Water flows at 2.0 m/s through a pipe of cross-section 0.010 m<sup>2</sup>, then enters a narrower section of 0.0040 m<sup>2</sup>. By continuity the speed there is

$$v_2 = \frac{A_1 v_1}{A_2} = \frac{0.010 \times 2.0}{0.0040} = 5.0 \text{ m/s}.$$

By Bernoulli's equation this faster stream is at **lower** pressure – the effect that lifts an aeroplane wing and pulls two passing ships together.

**Exam skill.** Choose the right law by what changes. If the pipe changes *width*, start with continuity ( $A_1 v_1 = A_2 v_2$ ) to get the speeds; if you then need a *pressure*, feed those speeds into Bernoulli. Watch the height term  $\rho gy$  only when the pipe also changes level.

## Exam tips

- Pressure with depth is  $P = P_0 + \rho gh$  — it depends on **depth only**, not the container's shape or width.

- **Buoyant force** = weight of fluid displaced ( $\rho_{\text{fluid}} g V_{\text{disp}}$ ); a floating object displaces its own weight, so the fraction submerged is  $\rho_{\text{object}}/\rho_{\text{fluid}}$ .
- Compare densities to predict floating vs sinking; a floating object is in equilibrium (buoyancy = weight), not weightless.
- Use **continuity**  $A_1 v_1 = A_2 v_2$ : a narrower pipe means faster flow.
- **Bernoulli**: where a fluid flows faster its pressure is lower (wing lift, spray).