

1.5 Vectors and Motion in Two Dimensions

Name: _____ Class: _____ Date: _____

Total: 12 marks**KEY WORDS** components 分量 • projectile's 抛体 • range 射程 • independent 相互独立 • resultant 合矢量

Objective

Build the skills to answer exam questions on **vectors and motion in two dimensions** — components and projectile motion.

You must be able to:

- resolve a 2-D vector into perpendicular **components** 分量 with $A_x = A \cos \theta$, $A_y = A \sin \theta$
- add vectors by combining components to find the **resultant** 合矢量 (magnitude and direction)
- explain that a **projectile's** 抛体 horizontal and vertical motions are **independent** 相互独立
- analyse projectile motion by applying the kinematic equations separately to x and y
- find the **range** 射程, maximum height, and time of flight

1 Worked examples

Study these first. Each one shows the method for a question type used later.

■ Resolving a vector

A force $A = 50 \text{ N}$ at 30° above the horizontal:

$$A_x = 50 \cos 30^\circ = 43 \text{ N}, \quad A_y = 50 \sin 30^\circ = 25 \text{ N}.$$

■ Independence of projectile motion

Horizontal motion is constant velocity, $v_x = v_0 \cos \theta$; vertical motion is free fall, $a_y = -g$. The two directions share only the **time**.

■ A projectile launched horizontally

A ball leaves a 20 m high table at 5.0 m s^{-1} (take $g = 10 \text{ m s}^{-2}$). Time to fall: $20 = \frac{1}{2}(10)t^2 \Rightarrow t = 2.0 \text{ s}$. Horizontal range = $5.0 \times 2.0 = 10 \text{ m}$.

2 Practice

2.1 A force of 80 N acts at 60° above the horizontal. Find its horizontal and vertical components. [2]

2.2 A ball rolls off a bench 1.25 m high at 3.0 m s^{-1} (take $g = 10 \text{ m s}^{-2}$). Find the time to land. [2]

2.3 Hence find how far from the base of the bench the ball lands. [1]

2.4 State what the horizontal and vertical motions of a projectile have in common. [1]

3 Exam-style questions

3.1 For a projectile (ignore air resistance), the horizontal component of velocity [1]

- **A** increases
- **B** decreases
- **C** stays constant
- **D** is zero

3.2 At the top of its path, a projectile's vertical velocity is [1]

- **A** maximum
- **B** zero
- **C** equal to its horizontal velocity
- **D** equal to g

3.3 A stone is thrown at 20 m s^{-1} at 30° above the horizontal (take $g = 10 \text{ m s}^{-2}$).

(a) Find the initial vertical velocity component. [1]

(b) Find the time to reach the top of the path. [1]

(c) Find the maximum height.

[2]

Solutions

2.1 $A_x = 80 \cos 60^\circ = 40 \text{ N}$; $A_y = 80 \sin 60^\circ = 69 \text{ N}$.

2.2 $1.25 = \frac{1}{2}(10)t^2 \Rightarrow t^2 = 0.25$, $t = 0.50 \text{ s}$.

2.3 $x = 3.0 \times 0.50 = 1.5 \text{ m}$.

2.4 the time of flight (both motions last the same time).

3.1 C.

3.2 B.

3.3 (a) $v_{0y} = 20 \sin 30^\circ = 10 \text{ m s}^{-1}$. (b) $t = 10/10 = 1.0 \text{ s}$. (c) $h = \frac{v_{0y}^2}{2g} = \frac{10^2}{20} = 5.0 \text{ m}$.