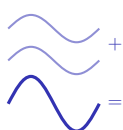


Superposition

AS Physics ■ Topic 8

A-Level Physics



Superposition

What we will cover

- 1 Principle of superposition
- 2 Stationary waves
- 3 Diffraction
- 4 Interference
- 5 The diffraction grating
- 6 Recap



1 Superposition

Superposition

Principle of superposition

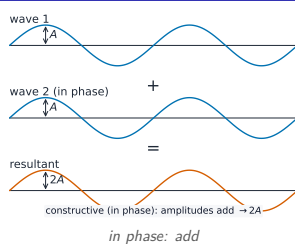
Where waves overlap, the displacement is the **vector sum** of each wave's displacement – and they then **pass through each other unchanged**.

in phase $A_1 + A_2$ – constructive interference 相长干涉	out of phase (π) amplitude $ A_1 - A_2 $ (destructive)
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Two equal waves in phase: $I \propto (2A)^2 = 4A^2$ – **four times** the intensity.

Superposition

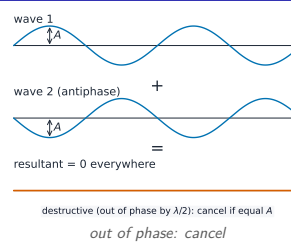
In phase: add



Crest 波峰 on crest: the two add, and the result is **constructive interference** 相长干涉.

Superposition

Out of phase: cancel

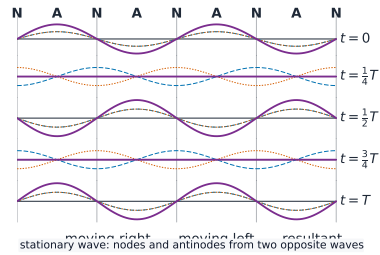


Crest on **trough** 波谷 – exactly in **antiphase** 反相 – gives **destructive interference** 相消干涉: they cancel.

2 Stationary waves

Superposition
Stationary waves

Stationary (standing) waves

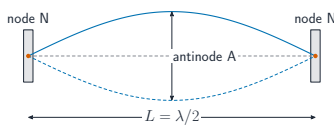


Two identical **progressive waves** 行波 travelling **opposite ways** overlap – usually a wave and its own **reflected** 反射 copy from a fixed end.

It stores energy but does **not** carry it along – the pattern stays put.

Superposition
Stationary waves

Nodes and antinodes



- **node** 波节 – always zero displacement
- **antinode** 波腹 – largest amplitude
- node to node = $\lambda/2$; node to antinode = $\lambda/4$

String 0.80 m, fixed ends, $v = 240 \text{ m s}^{-1}$

Fundamental: $\lambda = 2L = 1.60 \text{ m}$,
so $f = v/\lambda = 240/1.60 = 150 \text{ Hz}$.

Superposition
Stationary waves

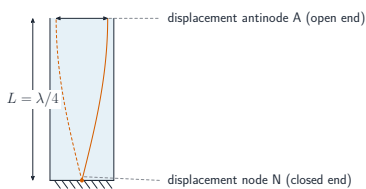
Measuring wavelength from node spacing

Drive a string with a vibrator at frequency f until a stationary pattern appears.

Measure the distance between two well-separated nodes and divide by the number of half-wavelengths 波长 between them.

Superposition
Stationary waves

Resonance in pipes



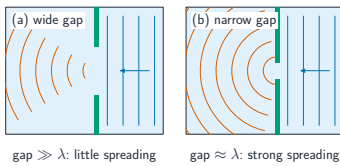
Resonance tube 共鸣管, closed one end:

- closed end = node, open end = antinode
- **fundamental** 基频: $L = \lambda/4$; next $L = 3\lambda/4$
- open both ends: fundamental $L = \lambda/2$

Then $v = f\lambda$ gives the wave speed.

3 Diffraction

Diffraction



Diffraction 衍射: a wave spreads after a gap or obstacle. Spread depends on λ vs gap width:

- gap $\gg \lambda$: little spread
- gap $\approx \lambda$: large spread

In a **ripple tank** 水波槽 the spread grows as the gap narrows. Same idea: you hear round a corner but cannot see round it.

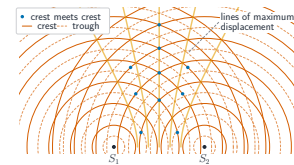
4 Interference

Interference and coherence

Interference 干涉: two **coherent** 相干 waves give a **steady** pattern. Coherent = constant phase difference (so the same frequency). Two lamps are not.

Make coherent light by passing **one** source through a **double-slit** 双缝 pair of **slits** 狭缝: both are lit by the same wavefront.

Interference and coherence, in detail



The pattern only stands still if the sources are **coherent**: same frequency, constant phase difference.

Four conditions for a clear fringe pattern

- 1 two **coherent** 相干 sources – a constant phase difference
- 2 roughly **equal amplitudes**, or the dark fringes are not dark
- 3 the waves **overlap** where you are looking
- 4 for light, the same plane of **polarisation** 偏振

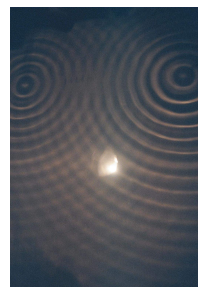
Miss any one and the fringes wash out – which is why two lamps show nothing.

Path difference

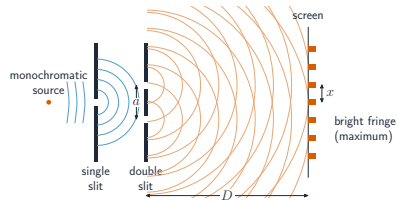
What happens at a point depends on the **path difference** 路程差 Δx :

bright: $\Delta x = n\lambda$

dark: $\Delta x = (n + \frac{1}{2})\lambda$



Young's double-slit experiment



Fringe spacing 条纹间距:

$x = \frac{\lambda D}{a}$ Smaller fringes: bigger a , smaller D , or bluer light.

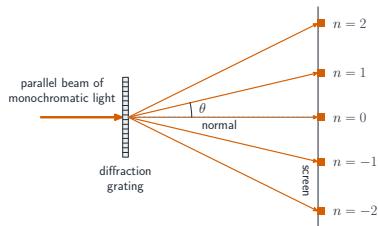
$$a = 0.50 \text{ mm}, \lambda = 600 \text{ nm}, D = 2.0 \text{ m}$$

$$x = (600 \times 10^{-9})(2.0) / (0.50 \times 10^{-3}) = 2.4 \text{ mm}$$

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Diffraction grating

The diffraction grating



Many slits, spacing d – maxima where

$$d \sin \theta = n\lambda.$$

$$500 \text{ lines/mm}, \lambda = 600 \text{ nm}, n = 1$$

$$d = 2.0 \mu\text{m}, \sin \theta = 0.30 \Rightarrow \theta \approx 17^\circ$$

A diffraction grating splits monochromatic light into sharp maxima on a screen

Working with a grating

slit spacing

$$N \text{ lines/mm} \Rightarrow d = 10^{-3}/N \text{ m}$$

highest order

$$n_{\text{max}} = \lfloor d/\lambda \rfloor: \text{ at } d/\lambda = 3.27 \text{ you see up to } n = 3, \text{ never } n = 4$$

sharper maxima

more slits add $\Rightarrow$ narrower, brighter lines than two slits

To find an unknown λ : shine it straight at the grating, measure θ_1 to the first-order maximum 极大, then $\lambda = d \sin \theta_1$. Averaging over higher orders cuts the error.

Exam tips

- Two-source interference: **constructive** when path difference $= n\lambda$, **destructive** when $= (n + \frac{1}{2})\lambda$; the sources must be **coherent**.
- Double slit: $\lambda = ax/D$; diffraction grating: $d \sin \theta = n\lambda$ – know every symbol.
- On a **stationary wave** mark nodes and antinodes; adjacent nodes are $\lambda/2$ apart; it stores energy but does not transfer it.
- A stationary wave needs two waves of the **same frequency travelling in opposite directions**.

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Recap

Topic 8 – key takeaways

1 Superposition

displacements add; in phase $4\times$ the intensity

3 Interference

coherent sources; $x = \lambda D/a$

2 Stationary waves

nodes & antinodes a $\lambda/2$ apart

4 Grating

$d \sin \theta = n\lambda$, sharp maxima

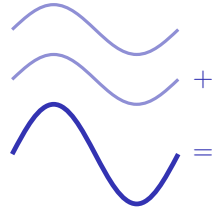
Check yourself

1 Distance between two next-door nodes?

2 What does “coherent” mean?

3 Path difference for a bright fringe?

4 Grating $d \sin \theta = n\lambda$ – which n is straight on?



Answers 1. $\lambda/2$ 2. constant phase difference 3. $\Delta x = n\lambda$ 4. $n = 0$