

Physical Quantities & Units

AS Physics ■ Topic 1

A-Level Physics

the length of an object



1.5 m

Physical Quantities & Units

What we will cover

- 1 Physical quantities
- 2 SI units & prefixes
- 3 Errors & uncertainties
- 4 Scalars & vectors
- 5 Recap & self-check



1 Physical quantities

Physical Quantities & Units

Physical quantities

A number *and* a unit

A **physical quantity** 物理量 has two parts:

- a **magnitude** 大小 – the number
- a **unit** 单位 – what the number means

The number alone tells you **nothing**.

1.5 m
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magnitude unit

"1.5" ❌

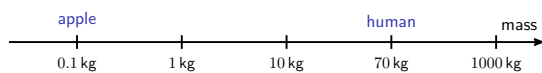
"1.5 m" ✅

Physical Quantities & Units

Physical quantities

Estimate the everyday

A good estimate has the right **order of magnitude** 数量级.



body weight $\approx 700 \text{ N}$

sound $\approx 340 \text{ m s}^{-1}$

light $\approx 3.0 \times 10^8 \text{ m s}^{-1}$

$g \approx 9.81 \text{ m s}^{-2}$

2 SI units

SI base quantities

The SI system has **seven base quantities** 基本量; these **five** are used here:

kg mass	m length	s time	A current	K temperature
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Combine them with $\times$ and $\div$ to get **every other unit** – N, J, W, Pa, ...

The seven estimates to know by heart

human mass 质量 70 kg	human weight 重力 700 N	human height 1.7 m	an apple 0.1 kg
speed of sound in air 340 m s^{-1}	speed of light in a vacuum 真空 $3.0 \times 10^8 \text{ m s}^{-1}$	free fall 自由落体 $g \approx 9.81 \text{ m s}^{-2}$	

An apple weighs about 1 N. That one number lets you check every other force estimate.

Build any derived unit

Each **derived unit** 导出单位 is just base units, from its defining equation:

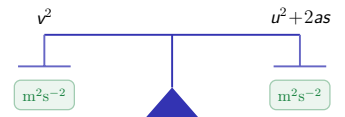
N newton 牛顿 force kg m s^{-2}	J joule 焦耳 energy $\text{kg m}^2 \text{s}^{-2}$	W watt 瓦特 power $\text{kg m}^2 \text{s}^{-3}$	Pa pascal 帕斯卡 pressure $\text{kg m}^{-1} \text{s}^{-2}$
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Read the unit straight off the defining equation: **speed** 速率 = m s^{-1} , **acceleration** 加速度 = m s^{-2} , and **stress** 应力 is force per area, so it takes the pascal too.

Do the units balance?

Homogeneous 量纲一致 = both sides have the **same base units**. Test $v^2 = u^2 + 2as$:

- LHS = $\text{m}^2 \text{s}^{-2}$
- $u^2 = \text{m}^2 \text{s}^{-2}$; $2as = \text{m}^2 \text{s}^{-2}$



Matching units don't **prove** an equation right – but **mismatched** units prove it wrong.

Prefixes – powers of ten

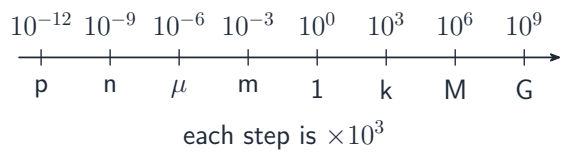
A **prefix** 词头 scales a unit by a power of ten.

n nano 10^{-9}	μ micro 10^{-6}	m milli 10^{-3}	1 base 10^0	k kilo 10^3	M mega 10^6	G giga 10^9
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each step is $\times 10^3$

← smaller larger →

Prefixes on the page



Each step is a factor of 1000, so converting is a shift of three places – never a new calculation.

Square the prefix too: $1 \text{ mm}^2 = (10^{-3} \text{ m})^2 = 10^{-6} \text{ m}^2$, not 10^{-3} .

Worked example – converting prefixes

$$0.25 \text{ kN mm}^{-2} \rightarrow \text{N m}^{-2}$$

Replace each prefix – and square the mm:

$$0.25 \frac{10^3}{(10^{-3})^2} = 2.5 \times 10^8 \text{ N m}^{-2}.$$

$$0.25 \text{ kN mm}^{-2}$$

replace prefixes
 $\times 10^3 / 10^{-6}$

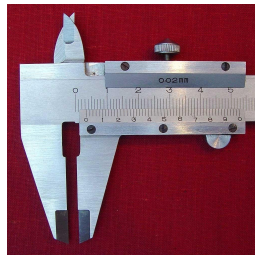
$$2.5 \times 10^8 \text{ N m}^{-2}$$

3 Errors and uncertainties

Every measurement is uncertain

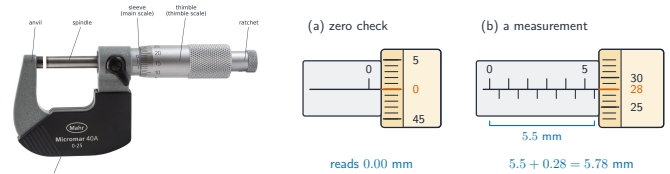
Every measurement carries some **uncertainty** 不确定度. A good experimenter:

- knows where it comes from
- estimates it fairly
- carries it to the answer



Calipers measure with a small uncertainty

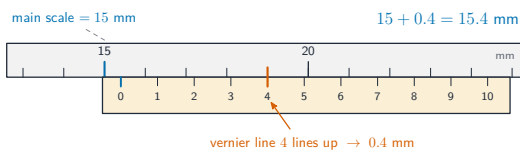
The micrometer – to 0.01 mm



Reading = sleeve (main scale) + thimble scale.

A micrometer 千分尺 reads to 0.01 mm: sleeve + thimble.

The vernier caliper – to 0.1 mm



Whole mm from the main scale
+ tenths from the lined-up
vernier mark.

Whole mm from the main scale, then tenths from the vernier mark that lines up.

Systematic vs random errors

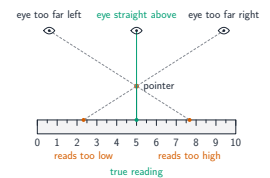
systematic error 系统误差 – same shift every time (**zero error** 零点误差, **calibration** 校准, **parallax** 视差).

Spoils the **accuracy**; repeating cannot find it.

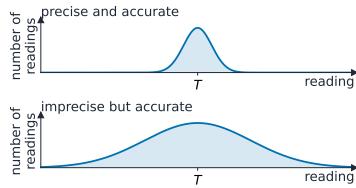


random error 随机误差 – scatters above and below with no pattern.

Spoils the **precision**; from how you read the scale, changing conditions, and the smallest step the **instrument** 仪器 shows. The **mean** 平均值 of many repeats cancels it.



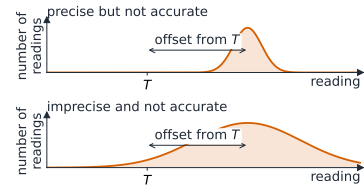
Precision 精密度: how narrow is the spread?



precision: how closely repeated readings agree (random error / spread)

precision 精密度: how narrow

Accuracy 准确度: is the peak on the true value?



accuracy: how close readings are to the true value (systematic error reduces accuracy)

accuracy 准确度: peak on true value?

Combining uncertainties

A **derived quantity** 导出量 is one you *calculate* from measured values. Each is $x \pm \Delta x$; its **percentage uncertainty** 百分比不确定度 = $\frac{\Delta x}{x} \times 100\%$.

- **add / subtract** $\Rightarrow$ add **absolute uncertainty** 绝对不确定度
- **multiply / divide** $\Rightarrow$ add the %
- **power** $a^n \Rightarrow$ multiply % by $|n|$

$$y = \frac{a b}{c}$$

$$\frac{\Delta y}{y} = \frac{\Delta a}{a} + \frac{\Delta b}{b} + \frac{\Delta c}{c}$$

Adding or subtracting – add the *absolute* uncertainties

$$\Delta y = \Delta a + \Delta b$$

Both $y = a + b$ and $y = a - b$ add them.

A **difference** keeps the whole Δ but has a far smaller value, so its % is the worst of the three.

$$a = (50.0 \pm 0.5) \text{ mm} \quad 1.0\%$$

$$b = (20.0 \pm 0.2) \text{ mm} \quad 1.0\%$$

$$a - b = (30.0 \pm 0.7) \text{ mm} \quad 2.3\%$$

one scale for all three – the *difference* is the widest

Multiplying or dividing – add the *percentage* uncertainties

$$\frac{\Delta y}{y} = \frac{\Delta a}{a} + \frac{\Delta b}{b} + \frac{\Delta c}{c}$$

Density $\rho = \frac{m}{V}$ from
 $m = (250 \pm 1) \text{ g}$ and
 $V = (100 \pm 2) \text{ cm}^3$.

The **bigger** % wins: improve V , not m .

$$\frac{\Delta m}{m} = \frac{1}{250} \quad 0.4\%$$

$$\frac{\Delta V}{V} = \frac{2}{100} \quad 2.0\%$$

$$\frac{\Delta \rho}{\rho} \quad 2.4\%$$

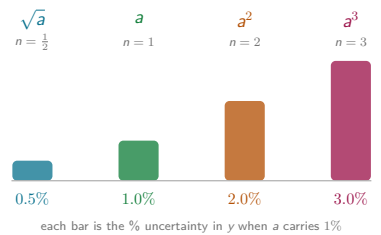
$$\rho = (2.50 \pm 0.06) \text{ g cm}^{-3}$$

Powers – multiply the percentage by the index

$$\frac{\Delta y}{|y|} = |n| \frac{\Delta a}{|a|}$$

A 1% error in a length becomes 3% in a volume – three edges each carry it.

Next slide: d carries 0.38%, so $V \propto d^3$ carries 1.14%.



Worked example – uncertainty in a volume

 $d = (5.26 \pm 0.02) \text{ cm}$ $V = \frac{\pi}{6} d^3 = 76.2 \text{ cm}^3$

1

% uncertainty in d

$$\frac{0.02}{5.26} \times 100\% = 0.38\%$$

2

$V \propto d^3$: triple it

$$3 \times 0.38\% = 1.14\%$$

3

back to absolute

$$1.14\% \times 76.2 = 0.9 \text{ cm}^3$$

$V = (76.2 \pm 0.9) \text{ cm}^3$

Significant figures

Give the answer the **same number of significant figures** 有效数字 as the least precise measurement you used – usually 2 or 3.

- too many $\Rightarrow$ looks too exact
- too few $\Rightarrow$ loses information

$76.234 \dots$

↓ drop extra

$76.2 \text{ cm}^3 \text{ (3 s.f.)}$

4 Scalars and vectors

Size only, or size *and* direction?

Scalar 标量

5 kg

magnitude only

mass · time · energy · speed
distance · **density 密度**
· **electric charge 电荷**

Vector 矢量



magnitude + direction

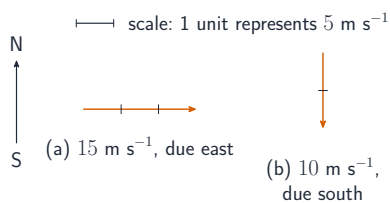
displacement 位移 · velocity
force · momentum 动量

Quick test – can you ask “in which direction?” If yes, it is a **vector**.

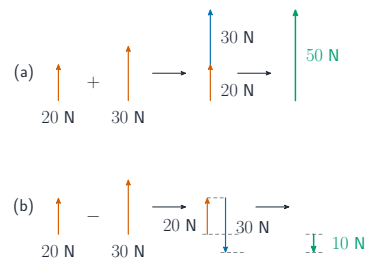
Drawing vectors to scale

A vector is an arrow:

- direction of arrow = direction
- length (to scale) = magnitude

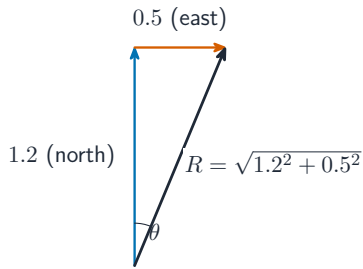


Adding tip to tail



- add **coplanar** 共面 vectors **tip to tail**
- the **resultant** 合矢量 runs first tail $\rightarrow$ last tip
- to subtract $\vec{X} - \vec{Y}$, add the reverse of $\vec{Y}$

Vectors at right angles



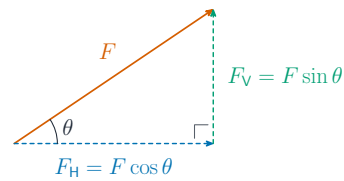
For **perpendicular** 垂直 vectors:

$$|\vec{R}| = \sqrt{X^2 + Y^2}, \quad \tan \theta = \frac{Y}{X}.$$

Swimmer

1.2 m s⁻¹ north, current
0.5 m s⁻¹ east:
 $|\vec{R}| = 1.3 \text{ m s}^{-1}$, $\theta \approx 23^\circ$ E of N.

Resolving into components



Split into two **perpendicular** 垂直 **components** 分量 – usually horizontal and vertical, or along and across a surface:

$$v_H = v \cos \theta, \quad v_V = v \sin \theta.$$

On an **inclined plane** 斜面:

$$W_{\parallel} = W \sin \theta, \quad W_{\perp} = W \cos \theta.$$

Exam tips

- Give every answer a **unit**, and check **homogeneity** – both sides of an equation must have the same base units.
- Distinguish **random error** (reduce by repeating and averaging) from **systematic error** (a zero or calibration error that repeats do not remove).
- Combine uncertainties: **add absolute** uncertainties when adding/subtracting, **add percentage** uncertainties when multiplying/dividing (and multiply the % by any power).
- Distinguish **precision** (small spread) from **accuracy** (close to the true value).
- Resolve a vector into perpendicular components ($F \cos \theta$, $F \sin \theta$); add vectors tip-to-tail or by components.

5

Recap

Topic 1 – key takeaways

1 Magnitude + unit

every quantity is a number *and* a unit

2 Derived units

built from 5 base units; check **homogeneity**

3 Precision vs accuracy

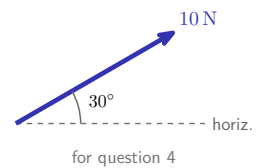
spread of repeats vs the true value

4 Vectors

add tip-to-tail; resolve into components

Check yourself

- 1 SI base units of the **pascal**?
- 2 Close, but far from true – precise or accurate?
- 3 $y = ab^2$ – how do the % combine?
- 4 10 N at 30° – horizontal component?



Answers 1. kg m⁻¹s⁻² 2. precise, not accurate 3. $\frac{\Delta y}{y} = \frac{\Delta a}{a} + 2 \frac{\Delta b}{b}$ 4. 8.7 N