

1 (a) Define gravitational potential at a point.

.....

 [2]

(b) Mars is a planet that may be considered to be an isolated uniform sphere of radius $3.4 \times 10^6 \text{ m}$.

A satellite of mass 122 kg is in orbit around Mars at a constant height of $1.7 \times 10^6 \text{ m}$ above the surface of the planet.

The height of the orbit is increased to $6.8 \times 10^6 \text{ m}$ above the surface. This increases the gravitational potential energy of the satellite by $5.1 \times 10^8 \text{ J}$.

(i) Show that the mass of Mars is $6.4 \times 10^{23} \text{ kg}$.

[3]

(ii) Calculate the gravitational potential ϕ at the surface of Mars. Give a unit with your answer.

$\phi = \dots\dots\dots$ unit $\dots\dots\dots$ [2]

(c) The satellite in (b) is moved to an orbit in which the satellite remains at the same point above the surface of Mars.

(i) The orbit has a period of 25 hours.

State what can be deduced from this about the rotation of Mars on its axis.

.....
 [1]

(ii) State **one** other feature of this orbit.

.....
 [1]

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1 (a) State Newton's law of gravitation.

.....

.....

..... [2]

(b) A planet may be considered as a uniform sphere.

A satellite is in circular orbit of period T around the planet at a height h above the surface. The height of the orbit can be adjusted by use of the satellite's rocket engines.

Fig. 1.1 shows the variation with h of $T^{\frac{2}{3}}$.

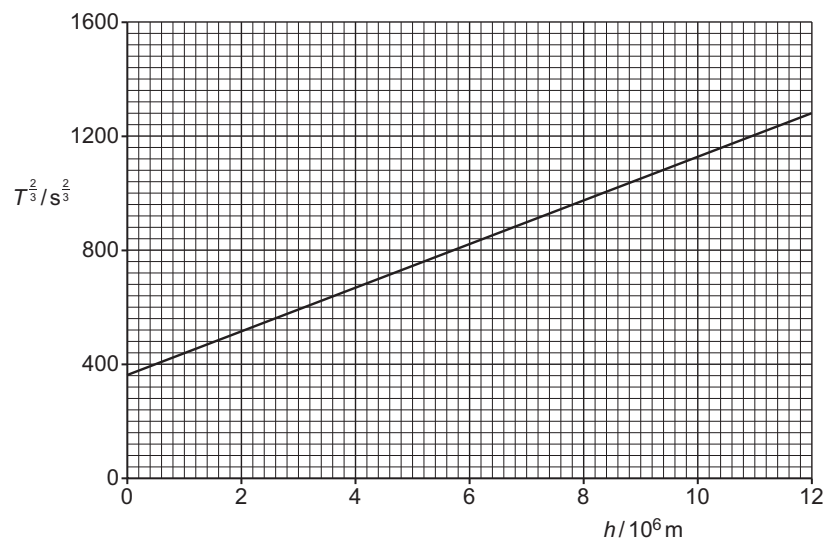


Fig. 1.1

(i) By reference to forces, explain why the orbit of the satellite is circular.

.....

.....

..... [2]

(ii) Use Newton's law of gravitation to show that h and T are related by

$$(h + B)^3 = \frac{GA}{4\pi^2} T^2$$

where G is the gravitational constant and A and B are constants that depend on the properties of the planet.

[3]

(iii) Use the gradient and intercept of the line in Fig. 1.1 to determine values for A and B . Give units with your answers.

$A =$ unit

$B =$ unit

[5]

[Total: 12]

1 (a) State Newton's law of gravitation.

.....

 [2]

(b) A satellite is in a circular orbit around a planet. The radius of the orbit is R and the period of the orbit is T . The planet is a uniform sphere.

Use Newton's law of gravitation to show that R and T are related by

$$4\pi^2 R^3 = GMT^2$$

where M is the mass of the planet and G is the gravitational constant.

[2]

(c) The Earth may be considered to be a uniform sphere of mass 5.98×10^{24} kg and radius 6.37×10^6 m.

A geostationary satellite is in orbit around the Earth.

Use the expression in (b) to determine the height of the satellite above the Earth's surface.

height = m [3]

(d) Another satellite is in a circular orbit around the Earth with the same orbital radius and period as the satellite in (c).

(i) Calculate the angular speed of the satellite in this orbit. Give a unit with your answer.

angular speed = unit [2]

(ii) Despite having the same orbital period, the orbit of this satellite is not geostationary.

Suggest **two** ways in which the orbit of this satellite could be different from the orbit of the satellite in (c).

1

 2
 [2]

[Total: 11]