

3 Vectors and the scalar product — Part 2

Name: _____ Class: _____ Date: _____

Vocabulary 词汇

Write each word three times. 把每个单词抄写三遍。

English	中文	Write it 3 times (English)
vector	向量	_____
magnitude	模长	_____
unit vector	单位向量	_____
scalar product	数量积	_____
perpendicular	垂直	_____

Recall

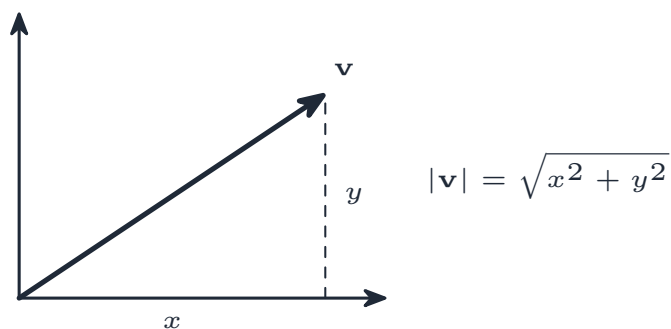
A **vector** 向量 has both size and direction. Pure 3 adds vectors in 3D and the scalar product.

New ideas

Read these first, then do the Practice.

■ 1 The magnitude of a vector

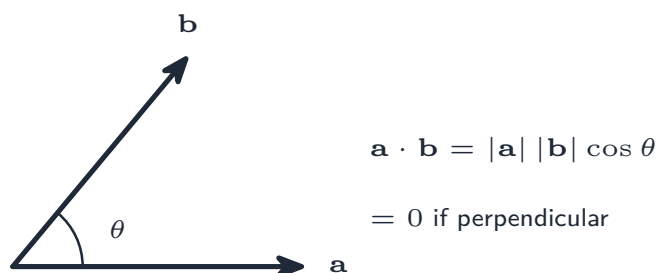
The **magnitude** 模长 (length) of a vector is found with Pythagoras:



$|v| = \sqrt{x^2 + y^2 + z^2}$. A **unit vector** 单位向量 has magnitude 1.

■ 2 The scalar product

The **scalar product** 数量积 (dot product) is linked to the angle between two vectors:



$a \cdot b = a_1b_1 + a_2b_2 + a_3b_3$. If $a \cdot b = 0$, the vectors are **perpendicular** 垂直.

Watch out: the magnitude uses Pythagoras: $|v| = \sqrt{x^2 + y^2 + z^2}$. The dot product $a \cdot b = 0$ means the vectors are *perpendicular*. To find the angle, use $a \cdot b = |a||b| \cos \theta$.

Practice

Try these in order.

3.6 Find the magnitude of the vector $3\mathbf{i} + 4\mathbf{j}$. [2]

3.7 What is the magnitude of a unit vector? [1]

3.8 Find $\mathbf{a} \cdot \mathbf{b}$ for $\mathbf{a} = (1, 2, 3)$ and $\mathbf{b} = (2, 0, 1)$. [2]

3.9 Two vectors have $\mathbf{a} \cdot \mathbf{b} = 0$. What does this tell you about them? [1]

3.10 Find the magnitude of $6\mathbf{i} + 8\mathbf{j}$. [1]

3.11 Challenge. Find the angle between $\mathbf{a} = (1, 0, 1)$ and $\mathbf{b} = (0, 1, 1)$, to the nearest degree. [3]