

They should be able to

1. carry out the process of **completing the square** for a quadratic polynomial $ax^2 + bx + c$ and use a completed square form
2. find the **discriminant** of a quadratic polynomial $ax^2 + bx + c$ and use the discriminant
3. solve **quadratic equations**, and **quadratic inequalities**, in one unknown
4. solve by substitution a pair of **simultaneous equations** of which one is linear and one is quadratic
5. recognise and solve equations in ax which are quadratic in some function of ax .
6. understand the terms **function**, **domain**, **range**, **one-one function**, **inverse function** and **composition of functions**
7. identify the **range** of a given function in simple cases, and find the **composition** of two given functions
8. determine whether or not a given function is **one-one**, and find the **inverse** of a one-one function in simple cases
9. illustrate in graphical terms the relation between a **one-one function** and its **inverse**
10. understand and use the **transformations** of the graph of $y = f(x)$ given by $y = f(x) + a$, $y = f(x + a)$, $y = af(x)$, $y = f(ax)$ and simple combinations of these.
11. find the equation of a **straight line** given sufficient information
12. interpret and use any of the forms $y = mx + c$, $y - y_1 = m(x - x_1)$, $ax + by + c = 0$ in solving problems
13. understand that the equation $(x - a)^2 + (y - b)^2 = r^2$ represents the **circle** with centre (a, b) and radius r
14. use algebraic methods to solve problems involving lines and circles
15. understand the relationship between a graph and its associated algebraic equation, and use the relationship between points of intersection of graphs and solutions of equations.
16. understand the definition of a **radian**, and use the relationship between radians and degrees
17. use the formulae $s = r\theta$ and $A = \frac{1}{2}r^2\theta$ in solving problems concerning the **arc length** and **sector area** of a circle.
18. sketch and use graphs of the **sine**, **cosine** and **tangent** functions (for angles of any size, and using either degrees or radians)
19. use the exact values of the **sine**, **cosine** and **tangent** of 30° , 45° , 60° , and related angles
20. use the notations $\sin^{-1} x$, $\cos^{-1} x$, $\tan^{-1} x$ to denote the **principal values** of the **inverse trigonometric relations**
21. use the identities $\frac{\sin \theta}{\cos \theta} \equiv \tan \theta$ and $\sin^2 \theta + \cos^2 \theta \equiv 1$
22. find all the solutions of simple **trigonometrical equations** lying in a specified interval (general forms of solution are not included).
23. use the expansion of $(a + b)^n$, where n is a positive integer
24. recognise **arithmetic** and **geometric progressions**
25. use the formulae for the n th term and for the sum of the first n terms to solve problems involving **arithmetic** or **geometric progressions**
26. use the condition for the **convergence** of a **geometric progression**, and the formula for the **sum to infinity** of a **convergent geometric progression**.
27. understand the **gradient** of a curve at a point as the limit of the gradients of a suitable sequence of chords, and use the notations $f'(x)$, $f''(x)$, $\frac{d^2y}{dx^2}$, and $\frac{d^2y}{dx^2}$ for first and second **derivatives**
28. use the **derivative** of x^n (for any rational n), together with constant multiples, sums and differences of functions, and of composite functions using the **chain rule**

29. apply differentiation to **gradients**, **tangents** and **normals**, increasing and decreasing functions and **rates of change**
30. locate **stationary points** and determine their nature, and use information about stationary points in sketching graphs.
31. understand **integration** as the reverse process of differentiation, and integrate $(ax + b)^n$ (for any rational n except -1), together with constant multiples, sums and differences
32. solve problems involving the evaluation of a **constant of integration**
33. evaluate **definite integrals**
34. use definite integration to find: - the **area** of a region bounded by a curve and lines parallel to the axes, or between a curve and a line or between two curves - a **volume of revolution** about one of the axes.

Stage	Use	Your notes
Starter 10 min · retrieval practice	Topic quiz 01 (10 questions, answers on sheet 2) Starter quiz 1 — past-paper questions	
Teach the new content	Handout 01 Slide deck 01 Vocabulary list 01	
Practice guided then independent	Exercise sheets 1.1, 1.2, 1.3, 1.4, 1.5, 1.6, 1.7, 1.8 Past-paper sheets 1.1, 1.2, 1.3, 1.4, 1.5, 1.6, 1.7, 1.8	
Check before they leave	Unit test 1 (with mark scheme)	
Homework set from the Library	Any unused exercise sheet above Holiday homework pack	

They should be able to

1. understand the meaning of $\frac{1}{x}$
2. divide a **polynomial**, of degree not exceeding 4, by a linear or quadratic **polynomial**, and identify the **quotient** and **remainder** (which may be zero)
3. use the **factor theorem** and the **remainder theorem**.
4. understand the relationship between **logarithms** and **indices**, and use the laws of **logarithms** (excluding change of base)
5. understand the definition and properties of e^x and $\ln x$, including their relationship as **inverse functions** and their graphs
6. use **logarithms** to solve equations and inequalities in which the unknown appears in **indices**
7. use **logarithms** to transform a given relationship to linear form, and hence determine unknown constants by considering the gradient and/or intercept.
8. understand the relationship of the **secant**, **cosecant** and **cotangent** functions to cosine, sine and tangent, and use properties and graphs of all six trigonometric functions for angles of any magnitude
9. use trigonometrical identities for the simplification and exact evaluation of expressions, and in the course of solving equations, and select an identity or identities appropriate to the context, showing familiarity in particular with the use of:
 - $\sec^2 \theta \equiv 1 + \tan^2 \theta$ and $\csc^2 \theta \equiv 1 + \cot^2 \theta$ – the expansions of $\sin(A \pm B)$, $\cos(A \pm B)$ and $\tan(A \pm B)$ – the formulae for $\sin 2A$, $\cos 2A$ and $\tan 2A$ – the expression of $a \sin \theta + b \cos \theta$ in the forms $R \sin(\theta \pm \alpha)$ and $R \cos(\theta \pm \alpha)$.
10. use the derivatives of e^x , $\ln x$, $\sin x$, $\cos x$, $\tan x$, together with constant multiples, sums, differences and composites
11. differentiate products and quotients
12. find and use the first derivative of a function which is defined parametrically or implicitly.
13.
 - extend the idea of ‘reverse differentiation’ to include the integration of e^{ax+b} , $\frac{1}{ax+b}$, $\sin(ax+b)$, $\cos(ax+b)$ and $\sec^2(ax+b)$
14.
 - use trigonometrical relationships in carrying out integration
15.
 - understand and use the **trapezium rule** to estimate the value of a definite integral.
16.
 - locate approximately a root of an equation, by means of graphical considerations and/or searching for a **sign change**
17.
 - understand the idea of, and use the notation for, a sequence of approximations which converges to a root of an equation
18.
 - understand how a given simple **iterative formula** of the form $x_{n+1} = \text{f}(x_n)$ relates to the equation being solved, and use a given iteration, or an iteration based on a given rearrangement of an equation, to determine a root to a prescribed degree of accuracy.

Stage	Use	Your notes
Starter 10 min · retrieval practice	Topic quiz 02 (10 questions, answers on sheet 2) Starter quiz 2 — past-paper questions	
Teach the new content	Handout 02 Slide deck 02 Vocabulary list 02	

Stage	Use	Your notes
Practice guided then independent	Exercise sheets 2.1, 2.2, 2.3, 2.4, 2.5, 2.6 Past-paper sheets 2.1, 2.2, 2.3, 2.4, 2.5, 2.6	
Check before they leave	Unit test 2 (with mark scheme)	
Homework set from the Library	Any unused exercise sheet above Holiday homework pack	

They should be able to

- understand the meaning of $\frac{p(x)}{q(x)}$
- divide a **polynomial**, of degree not exceeding 4, by a linear or quadratic polynomial, and identify the **quotient** and **remainder** (which may be zero)
- use the **factor theorem** and the **remainder theorem**
- recall an appropriate form for expressing rational functions in **partial fractions**, and carry out the decomposition, in cases where the denominator is no more complicated than $-(ax + b)(cx + d)(ex + f) - (ax + b)(cx + d)^2 - (ax + b)(cx^2 + d)$
- use the expansion of $(1 + x)^n$, where n is a rational number and $|x| < 1$
- understand the relationship between **logarithms** and **indices**, and use the laws of logarithms (excluding change of base)
- understand the definition and properties of e^x and $\ln x$, including their relationship as **inverse functions** and their graphs
- use logarithms to solve equations and inequalities in which the unknown appears in indices
- use logarithms to transform a given relationship to linear form, and hence determine unknown constants by considering the **gradient** and/or **intercept**.
- understand the relationship of the **secant**, **cosecant** and **cotangent** functions to cosine, sine and tangent, and use properties and graphs of all six trigonometric functions for angles of any magnitude
- use trigonometrical identities for the simplification and exact evaluation of expressions, and in the course of solving equations, and select an identity or identities appropriate to the context, showing familiarity in particular with the use of: $\sec^2 \theta \equiv 1 + \tan^2 \theta$ and $\operatorname{cosec}^2 \theta \equiv 1 + \cot^2 \theta$ – the expansions of $\sin(A \pm B)$, $\cos(A \pm B)$ and $\tan(A \pm B)$ – the formulae for $\sin 2A$, $\cos 2A$ and $\tan 2A$ – the expression of $a \sin \theta + b \cos \theta$ in the forms $R \sin(\theta \pm \alpha)$ and $R \cos(\theta \pm \alpha)$.
- use the derivatives of e^x , $\ln x$, $\sin x$, $\cos x$, $\tan x$, $\tan^{-1} x$, together with constant multiples, sums, differences and composites
- differentiate **products** and **quotients**
- find and use the first derivative of a function which is defined **parametrically** or **implicitly**.
- extend the idea of 'reverse differentiation' to include the integration of e^{ax+b} , $\frac{1}{ax+b}$, $\sin(ax+b)$, $\cos(ax+b)$, $\sec^2(ax+b)$ and $\frac{1}{x^2+a^2}$
- use trigonometrical relationships in carrying out integration
- integrate rational functions by means of decomposition into **partial fractions**
- recognise an integrand of the form $\frac{k f'(x)}{f(x)}$, and integrate such functions
- recognise when an integrand can usefully be regarded as a product, and use **integration by parts**
- use a given **substitution** to simplify and evaluate either a definite or an indefinite integral.
- locate approximately a **root** of an equation, by means of graphical considerations and/or searching for a **sign change**
- understand the idea of, and use the notation for, a sequence of approximations which **converges** to a root of an equation
- understand how a given simple **iterative formula** of the form $x_{n+1} = \text{f}(x_n)$ relates to the equation being solved, and use a given **iteration**, or an iteration based on a given rearrangement of an equation, to determine a root to a prescribed degree of accuracy.
- use standard notations for **vectors**, i.e. $\begin{pmatrix} x \\ y \end{pmatrix}$, $x\mathbf{i} + y\mathbf{j}$, $\begin{pmatrix} x \\ y \\ z \end{pmatrix}$, $x\mathbf{i} + y\mathbf{j} + z\mathbf{k}$, $\overrightarrow{AB}$, $\mathbf{a}$
- carry out addition and subtraction of vectors and multiplication of a vector by a **scalar**, and interpret these operations in geometrical terms

26. • calculate the **magnitude** of a vector, and use **unit vectors**, **displacement vectors** and **position vectors**
27. • understand the significance of all the symbols used when the equation of a straight line is expressed in the form $\mathbf{r} = \mathbf{a} + t\mathbf{b}$, and find the equation of a line, given sufficient information
28. • determine whether two lines are **parallel**, intersect or are **skew**, and find the point of intersection of two lines when it exists
29. • use formulae to calculate the **scalar product** of two vectors, and use scalar products in problems involving lines and points.
30. formulate a simple statement involving a **rate of change** as a **differential equation**
31. find by integration a general form of solution for a **first order differential equation** in which the variables are **separable**
32. use an **initial condition** to find a **particular solution**
33. interpret the solution of a **differential equation** in the context of a problem being modelled by the equation.
34. understand the idea of a **complex number**, recall the meaning of the terms **real part**, **imaginary part**, **modulus**, **argument**, **conjugate**, and use the fact that two complex numbers are equal if and only if both real and imaginary parts are equal
35. carry out operations of addition, subtraction, multiplication and division of two complex numbers expressed in **Cartesian form** $x + \text{i}y$
36. use the result that, for a polynomial equation with real coefficients, any non-real roots occur in **conjugate pairs**
37. represent complex numbers geometrically by means of an **Argand diagram**
38. carry out operations of multiplication and division of two complex numbers expressed in **polar form** $r(\cos \theta + \text{i}\sin \theta) \equiv r\text{e}^{\text{i}\theta}$
39. find the two **square roots** of a complex number
40. understand in simple terms the geometrical effects of conjugating a complex number and of adding, subtracting, multiplying and dividing two complex numbers
41. illustrate simple equations and inequalities involving complex numbers by means of **loci** in an **Argand diagram**

Stage	Use	Your notes
Starter 10 min · retrieval practice	Topic quiz 03 (10 questions, answers on sheet 2)	
Teach the new content	Handout 03 Slide deck 03 Vocabulary list 03	
Practice guided then independent	Exercise sheets 3.1, 3.2, 3.3, 3.4, 3.5, 3.6, 3.7, 3.8, 3.9 Past-paper sheets 3.1, 3.2, 3.3, 3.4, 3.5, 3.6, 3.7, 3.8, 3.9	
Check before they leave	Unit test 3 (with mark scheme)	
Homework set from the Library	Any unused exercise sheet above Holiday homework pack	

They should be able to

1. identify the forces acting in a given situation
2. understand the vector nature of force, and find and use components and resultants
3. use the principle that, when a particle is in equilibrium, the vector sum of the forces acting is zero, or equivalently, that the sum of the components in any direction is zero
4. understand that a contact force between two surfaces can be represented by two components, the normal component and the frictional component
5. use the model of a 'smooth' contact, and understand the limitations of this model
6. understand the concepts of **limiting friction** and **limiting equilibrium**, recall the definition of **coefficient of friction**, and use the relationship $F = \mu R$ or $F \leq \mu R$, as appropriate
7. use Newton's third law.
8. understand the concepts of **distance** and **speed** as **scalar** quantities, and of **displacement**, **velocity** and **acceleration** as **vector** quantities
9. sketch and interpret **displacement–time graphs** and **velocity–time graphs**, and in particular appreciate that – the area under a velocity–time graph represents displacement, – the gradient of a displacement–time graph represents velocity, – the gradient of a velocity–time graph represents acceleration
10. use **differentiation** and **integration** with respect to time to solve simple problems concerning displacement, velocity and acceleration
11. use appropriate formulae for motion with **constant acceleration** in a straight line.
12. use the definition of **linear momentum** and show understanding of its vector nature
13. use **conservation of linear momentum** to solve problems that may be modelled as the direct impact of two bodies.
14. • apply **Newton's laws of motion** to the linear motion of a particle of constant mass moving under the action of constant forces, which may include **friction**, **tension** in an inextensible string and **thrust** in a connecting rod
15. • use the relationship between **mass** and **weight**
16. • solve simple problems which may be modelled as the motion of a particle moving vertically or on an inclined plane with constant **acceleration**
17. • solve simple problems which may be modelled as the motion of **connected particles**.
18. • understand the concept of the **work done** by a force, and calculate the work done by a constant force when its point of application undergoes a displacement not necessarily parallel to the force
19. • understand the concepts of **gravitational potential energy** and **kinetic energy**, and use appropriate formulae
20. • understand and use the relationship between the change in energy of a system and the work done by the external forces, and use in appropriate cases the principle of **conservation of energy**
21. • use the definition of **power** as the rate at which a force does work, and use the relationship between power, force and velocity for a force acting in the direction of motion
22. • solve problems involving, for example, the **instantaneous acceleration** of a car moving on a hill against a resistance.

Stage	Use	Your notes
Starter	Topic quiz 04 (10 questions, answers on sheet 2)	
10 min · retrieval practice		

Stage	Use	Your notes
Teach the new content	Handout 04 Slide deck 04 Vocabulary list 04	
Practice guided then independent	Exercise sheets 4.1, 4.2, 4.3, 4.4, 4.5 Past-paper sheets 4.1, 4.2, 4.3, 4.4, 4.5	
Check before they leave	Unit test 4 (with mark scheme)	
Homework set from the Library	Any unused exercise sheet above Holiday homework pack	

They should be able to

- select a suitable way of presenting raw statistical data, and discuss advantages and/or disadvantages that particular representations may have
- draw and interpret **stem-and-leaf diagrams**, **box-and-whisker plots**, **histograms** and **cumulative frequency graphs**
- understand and use different measures of **central tendency** (mean, median, mode) and **variation** (range, interquartile range, standard deviation)
- use a cumulative frequency graph
- calculate and use the **mean** and **standard deviation** of a set of data (including grouped data) either from the data itself or from given totals Σx and Σx^2 , or coded totals $\Sigma(x - a)$ and $\Sigma(x - a)^2$, and use such totals in solving problems which may involve up to two data sets.
- understand the terms **permutation** and **combination**, and solve simple problems involving selections
- solve problems about arrangements of objects in a line, including those involving – repetition (e.g. the number of ways of arranging the letters of the word ‘NEEDLESS’) – restriction (e.g. the number of ways several people can stand in a line if two particular people must, or must not, stand next to each other).
- evaluate probabilities in simple cases by means of enumeration of equiprobable elementary events, or by calculation using **permutations** or **combinations**
- use addition and multiplication of probabilities, as appropriate, in simple cases
- understand the meaning of **exclusive** and **independent** events, including determination of whether events A and B are independent by comparing the values of $P(A \cap B)$ and $P(A) \times P(B)$
- calculate and use **conditional probabilities** in simple cases.
- draw up a **probability distribution** table relating to a given situation involving a **discrete random variable** X , and calculate $E(X)$ and $\text{Var}(X)$
- use formulae for probabilities for the **binomial** and **geometric** distributions, and recognise practical situations where these distributions are suitable models
- use formulae for the expectation and variance of the binomial distribution and for the expectation of the geometric distribution.
- understand the use of a **normal distribution** to model a **continuous random variable**, and use normal distribution tables
- solve problems concerning a variable X , where $X \sim N(\mu, \sigma^2)$, including: – finding the value of $P(X > x_1)$, or a related probability, given the values of x_1 , μ , σ . – finding a relationship between x_1 , μ and σ given the value of $P(X > x_1)$ or a related probability
- recall conditions under which the **normal distribution** can be used as an **approximation** to the **binomial distribution**, and use this approximation, with a **continuity correction**, in solving problems.

Stage	Use	Your notes
Starter 10 min · retrieval practice	Topic quiz 05 (10 questions, answers on sheet 2)	
Teach the new content	Handout 05 Slide deck 05 Vocabulary list 05	
Practice guided then independent	Exercise sheets 5.1, 5.2, 5.3, 5.4, 5.5 Past-paper sheets 5.1, 5.2, 5.3, 5.4, 5.5	

Stage	Use	Your notes
Check before they leave	Unit test 5 (with mark scheme)	
Homework set from the Library	Any unused exercise sheet above Holiday homework pack	

They should be able to

- use formulae to calculate probabilities for the distribution $\text{Po}(\lambda)$
- use the fact that if $X \sim \text{Po}(\lambda)$ then the mean and variance of X are each equal to λ
- understand the relevance of the **Poisson distribution** to the distribution of random events, and use the **Poisson distribution** as a model
- use the **Poisson distribution** as an approximation to the **binomial distribution** where appropriate
- use the **normal distribution**, with **continuity correction**, as an approximation to the **Poisson distribution** where appropriate.
- use, when solving problems, the results that $E(aX + b) = aE(X) + b$ and $\text{Var}(aX + b) = a^2\text{Var}(X)$ – $E(aX + bY) = aE(X) + bE(Y)$ – $\text{Var}(aX + bY) = a^2\text{Var}(X) + b^2\text{Var}(Y)$ for independent X and Y – if X has a **normal distribution** then so does $aX + b$ – if X and Y have independent **normal distributions** then $aX + bY$ has a **normal distribution** – if X and Y have independent **Poisson distributions** then $X + Y$ has a **Poisson distribution**.
- understand the concept of a **continuous random variable**, and recall and use properties of a **probability density function**
- use a **probability density function** to solve problems involving probabilities, and to calculate the **mean** and **variance** of a distribution.
- understand the distinction between a **sample** and a **population**, and appreciate the necessity for **randomness** in choosing samples
- explain in simple terms why a given **sampling method** may be unsatisfactory
- recognise that a **sample mean** can be regarded as a **random variable**, and use the facts that $E(\overline{X}) = \mu$ and that $\text{Var}(\overline{X}) = \frac{\sigma^2}{n}$
- use the fact that $\overline{X}$ has a **normal distribution** if X has a normal distribution
- use the **Central Limit Theorem** where appropriate
- calculate **unbiased estimates** of the population **mean** and **variance** from a sample, using either raw or summarised data
- determine and interpret a **confidence interval** for a population mean in cases where the population is normally distributed with known variance or where a large sample is used
- determine, from a large sample, an approximate **confidence interval** for a **population proportion**.
- understand the nature of a **hypothesis test**, the difference between **one-tailed** and **two-tailed** tests, and the terms **null hypothesis**, **alternative hypothesis**, **significance level**, **rejection region** (or **critical region**), **acceptance region** and **test statistic**
- formulate hypotheses and carry out a **hypothesis test** in the context of a single observation from a population which has a **binomial** or **Poisson distribution**, using – direct evaluation of probabilities – a normal approximation to the binomial or the Poisson distribution, where appropriate
- formulate hypotheses and carry out a **hypothesis test** concerning the population mean in cases where the population is normally distributed with known variance or where a large sample is used
- understand the terms **Type I error** and **Type II error** in relation to hypothesis tests
- calculate the probabilities of making **Type I** and **Type II errors** in specific situations involving tests based on a normal distribution or direct evaluation of binomial or Poisson probabilities.

Stage	Use	Your notes
Starter 10 min · retrieval practice	Topic quiz 06 (10 questions, answers on sheet 2)	
Teach the new content	Handout 06 Slide deck 06 Vocabulary list 06	
Practice guided then independent	Exercise sheets 6.1, 6.2, 6.3, 6.4, 6.5 Past-paper sheets 6.1, 6.2, 6.3, 6.4, 6.5	
Check before they leave	Unit test 6 (with mark scheme)	
Homework set from the Library	Any unused exercise sheet above Holiday homework pack	